OPERATING CHARACTERISTICS OF POROUS FLOATING – RING JOURNAL BEARINGS OPERATING WITH AN IMPROVED BOUNDARY CONDITIONS

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ABSTRACT

The static characteristics of porous floating ring journal bearing under hydrodynamic lubrication condition when operating with an improved boundary conditions are theoretically analyzed. An isothermal finite bearing theory was adopted during this analysis. The effect of different parameters, namely, permeability, geometrical dimensions of the ring and the bearing are considered. It was assumed that oil is supplied through the outside diameter of the bearing under low supply pressure. The angular extent of the oil – film formed in journal – ring and ring – bearing oil films was obtained by applying the integral momentum equation at the leading edge of the oil – film to define the beginning of the oil extent. While, the continuity of flow across the trailing edge was used to define the end of the oil extent. Numerical results show that the bearing performance affected by different parameters namely, permeability, eccentricity ratios of inner and outer oil – film, the clearance ratios, and the radii ratios.

KEY WORDS

hydrodynamic lubrication, floating ring, porous oil bearings, improved boundary conditions, slip velocity effect.

الخلاصة

يتضمن هذا البحث دراسة نظرية للخصائص السكانية للمسامات ذاتية التزويت ذات الحلقة العائمة. تم اعتماد نظرية الركائز المحددة الطول والتي تعمل تحت ظروف ثبوت درجة الحرارة لعرض أجزاء هذه الدراسة. تم الأخذ بنظر الاعتبار تأثير أداء السند بعدد من المؤثرات (التفاعلات، والشكل الهندسي للحلقة) ولضمان عمل الركيزة تحت الظروف الهيدروديناميكية فقد تم افتراس بان الركيزة تجهز بالزيت من القطر الخارجي للركيزة تحت ضغط تجهيز منخفض. و قد تم تحديد بداية و نهاية طبقة الزيت باستخدام معادلة الزخم التكاملية لتحقيق نهاية طبقة الزيت. وقد أظهرت نتائج الدراسة بان ضغط سالبا يولد قبل نهاية طبقة الزيت كما هو متوقع عند مقارنة النتائج مع تلك المنشرة لمكاسب الباحثين الذين عملوا على دراسة تصرف المسائد ذاتية التزويت. كما وأظهرت النتائج بان أداء السند يتأثر بمختلف العوامل وهي ضغط التجهيز، النفاذية، نسبة اللاتمروز، نسبة الخلوص، ونسبة أطوار قطر الحلقة.
INTRODUCTION

Over the past decades a considerable number of experimental and theoretical studies have been carried out to study the characteristics of the solid floating ring journal bearing. Isothermal fluid flow analysis assumes a constant lubricant viscosity had been made by Shaw and Nussdorfer (1987), Orcut and Ng (1987), Tanaka and Hori (1987), Rohde and Ezzat (1987), Li and Rohde (1987). An experimental investigation to the behaviour of floating ring journal bearing was carried out by Kettleborough as early as in (1961). He found that there are significant discrepancies between test data and predictions. Tatara (1987) noting that, over certain speed ranges and for high feed pressure, floating ring journal bearing operate in a stable mode. Dong and Zhao (1993), investigate the possibility of using the floating ring journal bearing in automotive application. They found that it is possible for floating ring bearings to be used in engines where the load non – stationary. Chong and Kim (1993), studied the operating characteristics of counter rotating floating ring journal bearings. It is theoretically confirmed that floating ring journal bearings can be used in counter rotating journal bearings. Andres and Kerth (1993) studied the thermal effect on the performance of the floating ring journal bearing for turbochargers application. It was found that the ring speed ratio decreases dramatically as shaft speed rises.

Lubrication performance characteristics of porous oil bearings (load capacity, friction coefficient, bearing temperature. etc.) have been the object of many recent investigations, Morgan and Cameron (1982); Rouleau (1987); Goldstein and Braun (1983); Cusano (1987); Reason and Dyer (1987); Prakash and Vij (1987). In the above investigations the half Sommerfeld condition was adopted. A theoretical and experimental work done by Kaneko et. al. (1992) shows that the oil film is formed mainly in the loaded part of the bearing and the angular extent of oil film is significantly smaller than that formed in a solid journal bearing even under hydrodynamic lubrication condition. Kaneko et. al. (1992) used an improved boundary conditions to obtain the angular position of leading a trailing ends of the oil film regions. They show that the negative pressure occur before the tailing end of the oil film region. Elsharkawy and Lotfi (1994) made an analysis to the hydrodynamic lubrication of porous bearings using a modified Brinkman – extended Darcy model. They found that the numerical model has been successfully predicting the experimental results of different researchers.

The angular extent of the oil – film formed in journal – ring and ring – bearing oil films is obtained by applying the integral momentum equation at the leading edge of the oil – film to define the beginning of the oil extent while, the continuity of flow across the trailing edge is used to define the end of the oil extent. The analysis of the bearing performance shows the occurrence of a negative film pressure before the trailing end of the oil – films region as expected when compared the results with the behaviour of porous bearings obtained by different workers.

So the purpose of this study is to analyze the steady state performance of porous floating ring journal bearing working under improved boundary conditions which are used to determine the leading and trailing edge of the oil films.

NUMERICAL ANALYSIS:
Model of the Porous Floating Ring Journal Bearing:

The porous floating ring journal bearing with the coordinate system used in this analysis can be shown in figure (1). The journal rotates with a constant angular velocity ($\omega_j$) about its axis while the porous ring rotates with an enhanced angular velocity ($\omega_r$) about its center. The porous bearing inserted into a solid housing having a circumferential groove in the middle. Lubricant oil at low supply pressure ($P_s$) is supplied to the groove in the middle.
PRESSURE DISTRIBUTION IN OIL FILM AND POROUS MATRIX:

The performance of the bearing inner and outer oil films are obtained from the following Reynolds’ equation for finite bearings including the so-called filter term and the effect of tangential slip velocity. For constant viscosity it can be written as, Kaneko et al.

\[
\frac{\partial}{\partial \theta} \left( h^3 \left( 1 + \zeta_1 \right) \frac{\partial P^*}{\partial \theta} \right)_ii + \left( \frac{D_{ii}}{L} \right)^2 \frac{\partial}{\partial Z} \left( h^3 \left( 1 + \zeta_1 \right) \frac{\partial P^*}{\partial Z} \right)_ii = 6 \frac{\partial}{\partial \theta} \left( h^3 \left( 1 + \zeta_0 \right) \right)_ii - 12 \Phi_{ii} \left( \frac{\partial P^*}{\partial r} \right)_{r=1} \right)_ii \]

\[
\left( \zeta_0 \right)_{ii} = \left( \frac{s}{\left( h^3 + s \right)} \right)_{ii} \]

\[
\left( \zeta_1 \right)_{ii} = \left[ 3 \left( h^3 s + 2 \alpha^2 s^2 \right) / \left( h^3 \left( h^3 + s \right) \right) \right]_{ii} \]

\[
(s)_{ii} = \left( \Phi_c / R \right)_{ii}^{1/2} / \alpha \]

\[
(\Phi)_{ii} = \left( k \cdot R / c^* \right)_{ii} \]

\[
\left( h^* \right)_{ii} = h_{ii} / c_{ii} = \left( 1 + \varepsilon \cos(\theta) \right)_{ii} \]

Fig. (1): Oil film region and oil flow of porous floating ring journal bearing
The slip coefficient ($\alpha$) is a dimensionless parameter which depends on the porous material. In the present analysis a value of ($\alpha$) as done in the previous studies, Cusano; Quan and Wang; Kaneko et. al.

Oil pressure in the porous ring and porous bearing is governed by the Darcy's equation which can be written in dimensionless form as follows Kaneko et. al.:

$$
\frac{1}{r_{ii}} \frac{\partial}{\partial r} \left( r^2 \frac{\partial \bar{P}^*}{\partial r} \right) + \frac{1}{r_{ij}^2} \frac{\partial^2 \bar{P}^*}{\partial^2 \theta} + \left( \frac{D_{ii}}{L} \right)^2 \frac{\partial^2 \bar{P}^*}{\partial^2 Z^2} = 0
$$

**BOUNDARY CONDITIONS:**

Two types of boundary conditions were used during this work.

**OIL FILM PRESSURE BOUNDARY CONDITIONS:**

The following boundary conditions were used to evaluate the pressure distribution through the oil films.

$$
\begin{align*}
\bar{P}^* (\theta_1, z^*)_{ii} &= \bar{P}^* (r, \theta_1, z^*)_{ii} = 0 \\
\bar{P}^* (\theta_2, z^*)_{ii} &= \bar{P}^* (r, \theta_2, z^*)_{ii} = 0 \\
\bar{P}^* (\theta, \pm 1)_{ii} &= \bar{P}^* (r, \theta, \pm 1)_{ii} = 0 \\
\bar{P}^* (\theta, z)_{ii} &= \bar{P}^* (r, \theta, z)_{ii} \quad \text{at} \quad (r^*) = 1 \\
\frac{\partial \bar{P}^* (\theta, 0)}{\partial Z^*} &= \bar{P}^* (\theta, r^*, 0) \\
\frac{\partial \bar{P}^* (\theta, 0)}{\partial Z^*} &= 0
\end{align*}
$$

The outer surface of porous matrix consists of two parts as shown in figure (1), the first is the part press – fitted inside the solid housing, where the pressure is evaluated from the condition that the permeability of the housing adjacent to the porous matrix is zero i.e.;

$$
\Phi = 0 \quad \text{or} \quad \frac{\partial \bar{P}^*}{\partial r^*} \quad ; \quad \text{at} \quad (r^*) \geq (r_o/r_i) \quad \text{and} \quad 0.5 \leq |Z^*| \leq 1
$$

The second is the part exposed to the circumferential groove in the housing, where the pressure is given by;

$$
\left( P^* \right)_2 = P^* = \frac{c_i^2 P_i}{(r^2 \eta \omega)_2} \quad \text{at} \quad (r^*) \quad \text{and} \quad |Z^*| \leq 0.5
$$

**CIRCUMFERENTIAL BOUNDARY CONDITIONS:**

The following boundary conditions are used to determine the oil film extent. The leading edge ($\theta_\cdot$) of the both oil films can be determined by extending the boundary condition used by Kaneko et. al. (1994), as follows:
\[
\begin{pmatrix}
M_{\theta_1} - M_{\theta_2} - M_{\theta_k} - M_{\theta_b}
\end{pmatrix}_{ii} = \cdot
\]

(11)

where;

\[M_{\theta_1}, M_{\theta_2}, M_{\theta_k} \text{ and } M_{\theta_b}\]  are the circumferential momentum flow rates across the control surfaces of the oil films, as shown in figure (\textsuperscript{1}). The momentum flow rates are given as follows:

\[
\begin{align*}
(M_{\theta_1})_{ii} &= 2 \int_0^{L/2} \int_0 \rho \left[ u_{\theta} | \theta \right]_{ii} dydz \\
(M_{\theta_2})_{ii} &= 2 \int_0^{L/2} \int_0 \rho \left[ u_{\theta} | \theta \right]_{ii} dydz \\
(M_{\theta_k})_{ii} &= 2(r_{ii}) \int_0^{\theta_k} \rho \left[ u_{\theta} | \theta \right]_{ii} dyd\theta \\
(M_{\theta_b})_{ii} &= 2(r_{ii}) \int_0^{L/2} \int_0 \rho \left[ u_{\theta} | \theta \right]_{ii} dyd\theta
\end{align*}
\]

(11)

The velocity components \((u_{\theta})_{ii}\) and \((u_z)_{ii}\) represent the components of the oil velocity in circumferential and axial directions in the both oil films, while \((u_r^*)_{jj}\) represents the radial velocity component of the oil inside the porous bearing and the porous ring. The values of \((\theta_1)_{ii}\) and \((\theta_2)_{ii}\) are assumed to be constant in \(z\) – direction.

\[\text{Fig. (\textsuperscript{1})}: \text{Circumferential momentum flow rates}\]

On the other hand the oil film extent at the trailing edge \((\theta_1)\) can be obtained by ensuring the continuity of the bulk flow a cross the boundary line at \((\theta_1)\).
\[ \left( \frac{q_{\theta_p}}{q_{\theta_c}} \right)_i = 0 \]

(1\textsuperscript{r})

where \( q_{\theta_p} \) and \( q_{\theta_c} \) are the flow rates across the trailing boundary line due to the Poiseuilles' flow and due to the Couettes' flow respectively. Equation (1\textsuperscript{r}) can be rewritten as:

\[
\left( \frac{q_{\theta_p}}{q_{\theta_c}} \right)_i = \left( \frac{1 + \xi}{6(1 + \xi_0)} \right) h^2 \oint_0^\infty \frac{1}{\partial \theta} \frac{d\theta}{d\zeta} \right|_{\theta=\theta_2} \]  

(1\textsuperscript{r4})

Knowing the values of \((\theta_1)_i\) and \((\theta_2)_i\) for each oil film (journal – ring and ring – bearing oil films), the angular extent of the first and second oil films \((\beta)_i\) are expressed in the form:

\[
(\beta)_i = (\theta_2)_i - (\theta_1)_i
\]

(1\textsuperscript{r6})

**BEARING PARAMETERS:**

Knowing the pressure distribution the dimensionless film force components along and perpendicular to the line of centers can be obtained, respectively as:

\[
W_R = -\int_{\theta_1}^{\theta_2} \left( P(\theta, z) \cos \theta \right) d\theta dz
\]

(1\textsuperscript{r5})

\[
W_T = \int_{\theta_1}^{\theta_2} \left( P(\theta, z) \sin \theta \right) d\theta dz
\]

(1\textsuperscript{r7})

the total dimensionless load can be expressed as:

\[
W = \sqrt{W_R^2 + W_T^2}
\]

(1\textsuperscript{r8})

The attitude angle \((\Psi)_i\) can be evaluated as:

\[
(\Psi)_i = \tan^{-1} \left( \frac{W_T}{W_R} \right)_i
\]

(1\textsuperscript{r9})

The friction force on the inner and outer surfaces of the ring can be evaluated as;


\[ F_{ii}^\wedge = \int_0^\theta_2 \int_0^\theta_1 \frac{h_{ii}^\wedge}{2} \frac{\partial P_{ii}^\wedge}{\partial \theta} \, d\theta \, dz^\wedge + \int_0^\theta_2 \int_0^\theta_1 \frac{h_{ii}^\wedge}{2} \frac{\xi_1 \theta}{3} \frac{\partial P_{ii}^\wedge}{\partial \theta} \, d\theta \, dz^\wedge + \int_0^\theta_2 \int_0^\theta_1 \frac{1+\xi_0 \theta}{h_{ii}^\wedge} \, d\theta \, dz^\wedge \]  

\[ (\mu^\wedge)_{ii} = \frac{\left(F_{r}^\wedge\right)_{ii}}{\left(W\right)_{ii}} \]  

**(STEADY STATE PERFORMANCE):**

To calculate the steady state performance of the bearing it is necessary to find out the steady state equilibrium position of the journal and ring centers, the following conditions for moments and forces are hold for equilibrium state.

\[ T_{inner}^\wedge = T_{outer}^\wedge \]

where,

\[ T_{ii}^\wedge = \int_0^\theta_2 \int_0^\theta_1 \frac{h_{ii}^\wedge}{2} \frac{\partial P_{ii}^\wedge}{\partial \theta} \, d\theta \, dz^\wedge + \int_0^\theta_2 \int_0^\theta_1 \frac{h_{ii}^\wedge}{2} \frac{\xi_1 \theta}{3} \frac{\partial P_{ii}^\wedge}{\partial \theta} \, d\theta \, dz^\wedge + \int_0^\theta_2 \int_0^\theta_1 \frac{1+\xi_0 \theta}{h_{ii}^\wedge} \, d\theta \, dz^\wedge \]  

The second equilibrium conditions which specify the steady state performance of the bearing is the force balance which state that;

\[ W_1^\wedge = W_2^\wedge \]

The ring speed to the journal speed can be found from the torque equilibrium as follows;

\[ \frac{N_r}{N_j} = \frac{T_{inner}^\wedge R_1^3}{T_{outer}^\wedge R_2^3} \frac{c_2}{c_1} \]  

**(METHOD OF SOLUTION):**

Oil film pressure distribution and the oil pressure distribution through the porous matrix can be obtained by solving equations (\( ^\wedge \)) and (\( ^\wedge \)) simultaneously. These equations are discretized and solved simultaneously with an appropriate boundary conditions. In the present analysis (\( ^\wedge \)) divisions in circumferential direction (\( N_1 \)), divided into (\( ^\wedge \)) divisions for the rupture zone and
(\textsuperscript{\textbullet}) divisions for the effective zone. Sixteen divisions in axial direction (N_{\text{r}}) and eight divisions in radial direction (N_{\text{r}}) have been adopted. The governing equations are transformed to discrete form using finite difference technique and then solved iteratively with successive under relaxation factor, to obtain the pressure and the location of the inlet and trailing boundary lines for the oil–film regions, the iterations are continued until the following inequalities are satisfied simultaneously,

\[
\left| \sum \sum \left( P_{i,j,k}^{n+1} - P_{i,j,k}^{n} \right) \right|_{ij} < 10^{-5} \\
\left| \sum \sum \left( P_{i,j,k}^{n+1} - P_{i,j,k}^{n} \right) \right|_{ij} < 10^{-5}
\]

\[ (\text{IV}) \]

\[
\left| M_{\theta_1}^{\hat{\theta}} - M_{\theta_2}^{\hat{\theta}} - M_{\theta_0}^{\hat{\theta}} - M_{\theta_k}^{\hat{\theta}} / M_{\theta_h}^{\hat{\theta}} \right|_{i\theta} < 10^{-3}
\]

\[ (\text{V}) \]

\[
\left| q_{\theta_0} / q_{\theta_1} \right|_{ii} = \left| \left( \frac{1 + \zeta_1}{6(1 + \zeta_0)} \right) - \frac{1}{6} \left( \frac{P_x^{\hat{\theta}}}{\theta = \theta_0} \right) \right|_{ii} < 10^{-3}
\]

\[ (\text{VI}) \]

To ensure the steady state performance of the bearing, the following equilibrium conditions must be satisfied:

- torque equilibrium:

\[
\left| T_{\text{inner}} - T_{\text{outer}} \right| < 10^{-3}
\]

\[ (\text{VII}) \]

- load equilibrium:

\[
\left| W_{1}^{\hat{\theta}} - W_{2}^{\hat{\theta}} \right| < 10^{-3}
\]

\[ (\text{VIII}) \]

Always (n) and (n+1) used in above equations denote two consecutive iterations and the points i, j, k represent the grid number in radial, circumferential, and axial directions respectively.
where:

\[
\begin{align*}
\left( \hat{M}_{\theta_i} \right)_{ii} &= \left( M_{\theta_i} \right)_{ii} f \left( \rho \theta_i r_i^2 \omega_i^2 L \right) = \left[ \int_0^1 \left( h_i^{\hat{\alpha}} \left( \frac{\partial P^*}{\partial \theta} \right) \left( \frac{\partial P^*}{\partial r} \right)^2 \left( 9 + 15 \zeta_1 + 10 \zeta_2 \right) \right) dZ^* \right]_{ii} \\
&= -1 \left[ \int_0^1 \left( h_i^{\hat{\alpha}} \left( \frac{\partial P^*}{\partial \theta} \right) \left( 3 + 3 \zeta_0 + 2 \zeta_1 + 4 \zeta_0 \zeta_1 \right) \right) dZ^* \right]_{ii} + \left[ \int_0^1 \left( \frac{h_i^{\hat{\alpha}}}{3} \left( 1 + \zeta_0 + \zeta_2 \right) \right) dZ^* \right]_{ii} \\
\left( \hat{M}_{\theta_2} \right)_{ii} &= \left( M_{\theta_2} \right)_{ii} f \left( \rho \theta_i r_i^2 \omega_i^2 L \right) = \left[ \int_0^1 \left( h_i^{\hat{\alpha}} \left( \frac{\partial P^*}{\partial \theta} \right) \left( 9 + 15 \zeta_1 + 10 \zeta_2 \right) \right) dZ^* \right]_{ii} \\
&= -1 \left[ \int_0^1 \left( h_i^{\hat{\alpha}} \left( \frac{\partial P^*}{\partial \theta} \right) \left( 3 + 3 \zeta_0 + 2 \zeta_1 + 4 \zeta_0 \zeta_1 \right) \right) dZ^* \right]_{ii} + \left[ \int_0^1 \left( \frac{h_i^{\hat{\alpha}}}{3} \left( 1 + \zeta_0 + \zeta_2 \right) \right) dZ^* \right]_{ii} \\
\left( \hat{M}_{\theta_3} \right)_{ii} &= \left( M_{\theta_3} \right)_{ii} f \left( \rho \theta_i r_i^2 \omega_i^2 L \right) = \left[ \frac{1}{72} \left( \frac{D_i L}{\theta_i} \right)^2 \omega_i^2 L \right]_{ii} \\
A &= h_i^{\hat{\alpha}} \left( 3 + 3 \zeta_0 + 2 \zeta_1 + 4 \zeta_0 \zeta_1 \right) \left( \frac{\partial P^*}{\partial Z} \right)_{Z=1} \leq 0 \quad \text{if} \quad \left( \frac{\partial P^*}{\partial Z} \right)_{Z=1} \leq 0 \\
A &= 0 \quad \text{if} \quad \left( \frac{\partial P^*}{\partial Z} \right)_{Z=1} > 0 \\
\left( \hat{M}_{\theta_3} \right)_{ii} &= \left( M_{\theta_3} \right)_{ii} f \left( \rho \theta_i r_i^2 \omega_i^2 L \right) = \left[ \frac{1}{72} \left( \frac{D_i L}{\theta_i} \right)^2 \omega_i^2 L \right]_{ii} dZ^* \\
\left( B \right)_{ii} &= \left( \Phi \left( \frac{h_i^{\hat{\alpha}}}{12} \left( 1 + \zeta_1 \right) \left( \frac{\partial P^*}{\partial \theta} \right) - \frac{1}{2} \left( 1 + \zeta_3 \right) \right) \right) \left( \frac{\partial P^*}{\partial r} \right)_{r=1} \leq 0 \quad \text{if} \quad \left( \frac{\partial P^*}{\partial r} \right)_{r=1} \leq 0 \\
\left( B \right)_{ii} &= \left( \frac{c}{r} \Phi \left( \frac{h_i^{\hat{\alpha}}}{12} \left( 1 + \zeta_1 \right) \left( \frac{\partial P^*}{\partial \theta} \right) - \frac{1}{2} \left( 1 + \zeta_3 \right) \right) \right) \left( \frac{\partial P^*}{\partial r} \right)_{r=1} \leq 0 \quad \text{if} \quad \left( \frac{\partial P^*}{\partial r} \right)_{r=1} \leq 0 \\
\end{align*}
\]

RESULTS AND DISCUSSION:

Figures (\textsuperscript{a}-a) and (\textsuperscript{a}-b) represents a comparison between the results obtained using the computer program which prepared and written in FORTRAN – \textsuperscript{a} \textsuperscript{a} \textsuperscript{a} language and executed on a
personal computer (Pentium 2) of 5MB Ram, through this work with that obtained from the published data in Kaneko et., al., (14). The solution of porous floating ring journal bearing merely consists of parallel solutions of two ordinary porous bearings via the mobility method it can be shown that the average percentage of error evaluated is (1%).

Figure (4) shows that the oil film has a higher peak of pressure as the supply pressure increases, which can be attributed to the higher flow of oil out of the porous matrix. The oil film pressure increases with increasing the supply pressure and clearance ratio and decreasing the radii ratio as shown in figures (4, 5). An increased oil film extent has been shown in this case.

The correlation between (ε1) and (ε2) can be shown in Figure (7 and 8). It is clear that (ε1) some times become greater than (ε2) and vice versa. This correlation affected by different parameter, namely, permeability, clearance ratio and radii ratio. This is true to maintain the equilibrium condition of the bearing and to ensure that the bearing is hydrodynamically lubricated.

The correlation between the ring – bearing and the journal – ring eccentricity ratios is affected by the radii ratio as shown in Figure (9). It is clear that the ring – bearing eccentricity ratio becomes lower than the journal – ring eccentricity ratio for a bearing with a ring of radii ratio is less than (1, 2) while, the ring – bearing eccentricity ratio become greater than the journal – ring eccentricity ratio for a ring with a radii ratio grater than (1, 2). This is true to maintain the steady state performance of the bearing. Also the ring speed becomes greater as the radii ratio decreases which make (ε1) greater than (ε2) in this case.

The oil films extent increases with increasing values of the permeability as shown in figures (10 and 11). This is can be explained by knowing that the oil flow from the porous matrix increases in this case.

The coefficient of friction increases with higher values of permeability of the porous matrix as shown in figures (12 and 13). The values of the Sommerfeld number which give the minimum friction decreases with decreasing the values of the permeabilities.

Fig. (10-a), Comparison Between Experimental Published Results Kaneko, (14) with the Results obtained in the Present Work for Pressure Distribution at $P_s = 0.1$.

Figure (10-b), Comparison Between Published Results [14] with the Results obtained in the Present Work for Oil – Film Extent.
Fig. (1), Computed Results for Circumferential Pressure Distribution in Ring – Bearing Clearance Gap for Various Values of Dimensionless Oil – Feed Pressure.

Fig. (2), Circumferential Pressure Distribution in Ring – Bearing Clearance Gap for Various Values of Clearance Ratios.

Fig. (3), Circumferential Pressure Distribution in Ring – Bearing Clearance Gap for Different Values of Radii Ratios.

Fig. (4), Correlation Between Journal Eccentricity Ratio ($\varepsilon_1$) and Ring Eccentricity Ratio ($\varepsilon_2$) for Different Values of Permeability.
Fig. (a), Correlation Between Journal Eccentricity Ratio ($\varepsilon_j$) and Ring Eccentricity Ratio ($\varepsilon_r$) for Different Values of Clearance Ratio.

Fig. (b), Correlation Between Journal Eccentricity Ratio ($\varepsilon_j$) and Ring Eccentricity Ratio ($\varepsilon_r$) for Different Values of Radii Ratio.

Fig. (c), Outer Oil – Film Extent Versus Sommerfeld Number for Various Values of permeability parameter.

Fig. (d), Inner Oil – Film Extent Versus Sommerfeld Number for Various Values of permeability parameter.
CONCLUSIONS:

From the previous analysis the following can be concluded:

1- The load carrying capacity increases with increasing the values of the supply pressure and clearance ratio.

2- The load carrying capacity increases for the floating ring journal bearing working with ring has lower radii ratio.

3- The journal – ring eccentricity ratio become higher than the ring – bearing eccentricity ratio for bearings of higher permeability, clearance ratio and lower radii ratio.

4- The oil – film extent increases with decreasing the values of the radii ratio.

5- The minimum coefficient of friction decreases with increasing the values of the supply pressure and the clearance ratio. The minimum value of the friction coefficient decreases with decreasing the values of the radii ratio.

REFERENCES:


The following symbols are used throughout this work.

\( c_j \) Journal – Ring Mean Radial Clearance (m)
\( c_y \) Ring – Bearing Mean Radial Clearance (m)
\( \theta_i \) Dimensionless Film Thickness, \( h^\theta = h/c \)
\( \eta_i \) Permeability of the Porous Matrix (m\(^{-1}\))
\( L \) Length of the Ring and the Bearing Length (m)
\( M_{\theta i} \) Circumferential Momentum Flow Rate across Oil Film Surface at Inlet End of Oil – Film Region, \( \theta_i \)
\( M_{\theta j} \) Dimensionless Circumferential Momentum Flow Rate across Oil – Film Surface at Inlet End of Oil–Film Region, i.e. at \( \theta_i \)
\( M_{j i} \) Circumferential Momentum Flow Rate across Oil – Film Surface at Trailing End of Oil – Film Region, i.e. at \( \theta_j \)
\( M_{\theta c} \) Dimensionless Circumferential Momentum Flow Rate across Oil – Film Surface at Both Axial Ends (z = ±L/\( \eta \))
\( M_{\theta b} \) Dimensionless Circumferential Momentum Flow Rate across Oil – Film Surface at Both Axial Ends i.e. at \( (z = \pm L/\eta) \), \( \theta_b \)
\( N_j \) Journal Rotational Speed (r.p.m)
\( N_f \) Floating Ring Rotational Speed (r.p.m)
\( P' \) Dimensionless Oil-Film Pressure, \( P' = \rho c/(R^\theta \eta \omega) \)
\( P^{*} \) Dimensionless Oil – Film Pressure Inside the Porous Matrix, \( P^* = c' P'/ (R^\theta \eta \omega) \)
\( P_s \) Supply Pressure (N/m\(^2\))
\( \eta \) Normalized radial coordinate, \( \eta = r/R_e \)
\( R_j \) Journal Radius(m)
\( S \) Sommerfeld Number, \( S = (R \eta \omega L / W) (R / c)^\eta \)
\( s \) Slip parameter
Dimensionless Frictional Torque, $T^\circ = T c / \eta \omega R L$

Journal Velocity (m/s)

Ring Velocity (m/s)

Oil–Film Velocity Components in \(\theta, r, z\) Directions Respectively (m/s)

Oil Velocity Components inside the Porous Matrix in \(\theta, r, z\) Directions Respectively (m/s)

Dimensionless Load Carrying Capacity, $(W^r)_{ii} = (W c R / \eta \omega R L)_{ii}$

Dimensionless Component of Oil–Film Force Along the Line of Centers,

Dimensionless Component of Oil–Film Force Perpendicular to the Line of Centers

Normalized axial coordinate, $Z^\circ = z/(L/\tau)$

**Greek Symbols**

Eccentricity Ratio

Absolute Viscosity of Oil (pa . s)

Angular Coordinate from Maximum Film Thickness Position (Degree)

Dimensionless Friction Coefficient $(\mu^r)_{ii} = (R/c)\mu_{ii}$

Density of oil (kg/m$^3$)

Permeability parameter, $(\Phi)_{ii} = (k R / c^r)_{ii}$

Attitude Angle (degrees)

**Subscript**

b Referring to Bearing

ii =\^tor referred for Journal – Ring Oil – Film

=\^tor referred for Ring – bearing Oil – Film

jj =\^tor for Porous Matrix of Floating Ring

=\^tor for Porous Matrix of Bearing

j Referring to Journal