

Engineering Surveying

3rd Stage

Horizontal Curve

Luma Khalid

E-mail : [luma.k@coeng.uobaghdad .edu.iq](mailto:luma.k@coeng.uobaghdad.edu.iq)

Horizontal Plan

Horizontal Plan

Straight lines have fixed direction

Horizontal Curves

Circular Curves

Spiral Curves

Simple

Clothoid

Compound

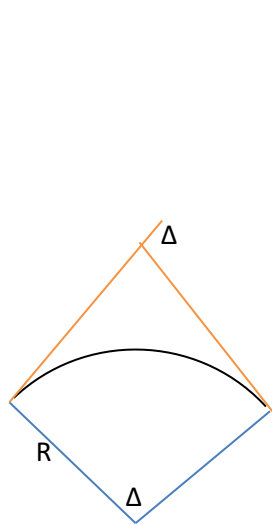
Cubic Parabola

Reverse

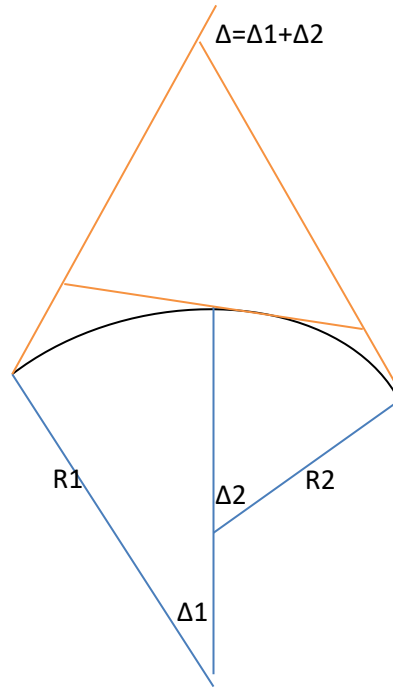
Cubic Spiral

Lemniscate

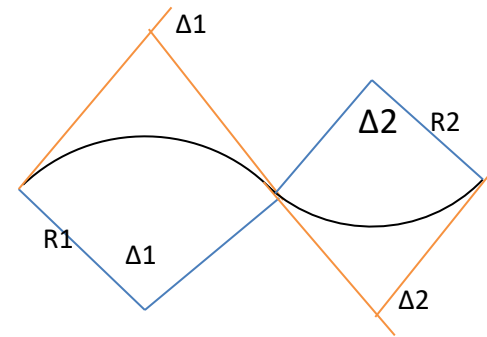
Circular Curves



Simple

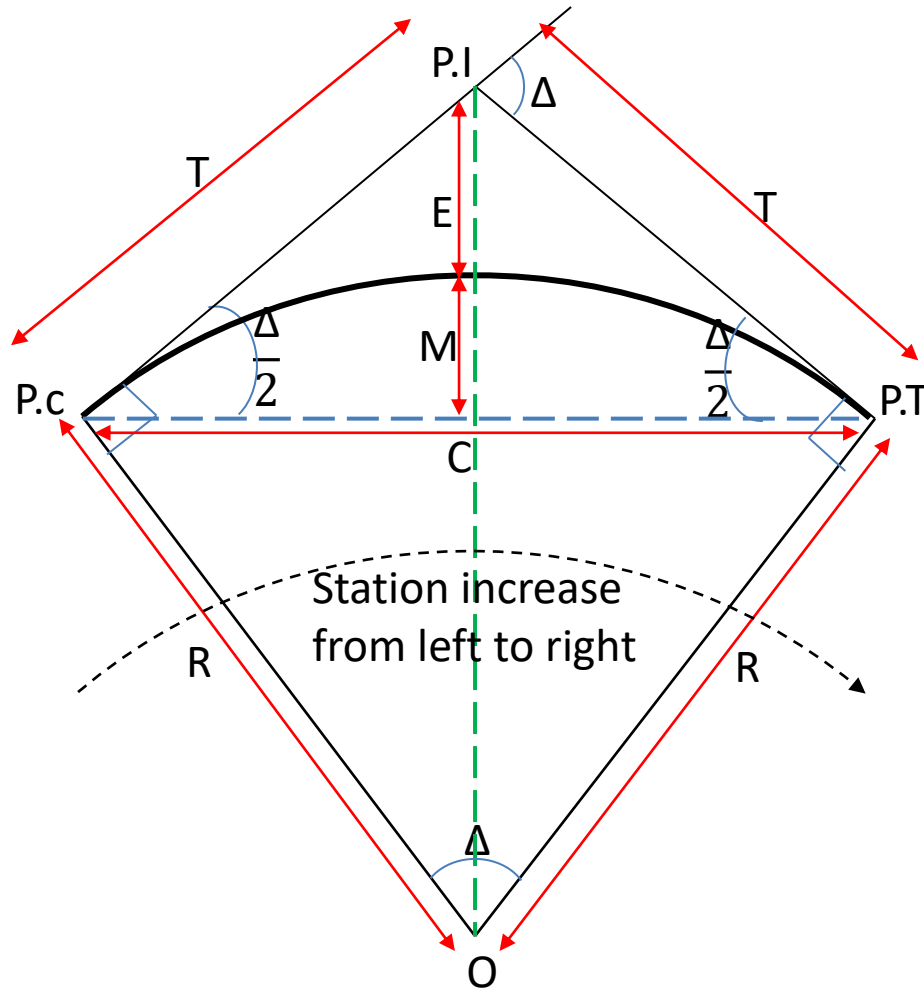


Compound



Reverse

Simple Circular Curve



Symbols & Terms of Simple Circular Curve

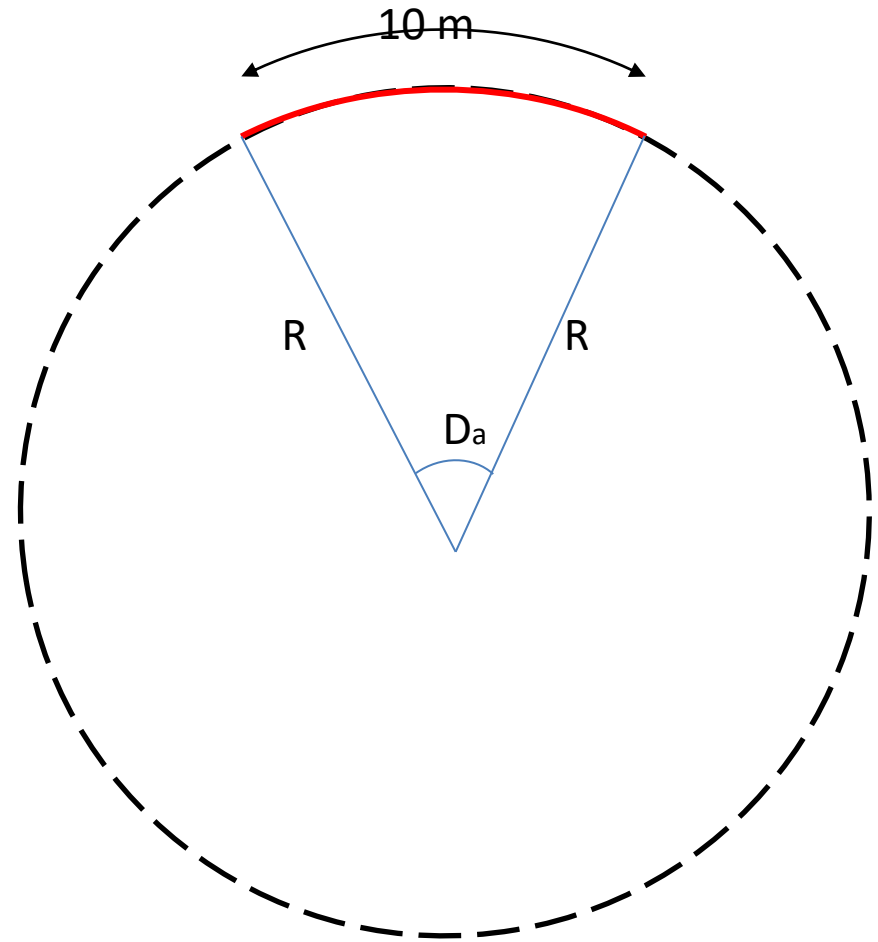
- Δ = Intersection angle , Deflection angle or Central angle
- R= Radius of curve
- T =Tangent length
- L= length of curve
- C= Chord length or L.C=long chord
- M=Middle distance
- E=External distance
- P.C=Point of curvature or B.C=Beginning of curve or T.C=Tangent to curve point
- P.I=Point of intersection or V=Vertex or I.P=Intersection point
- P.T=Point of tangency or E.C=End of curve or C.T=Curve to tangent point
- D=Degree of curve or Degree of curvature

Degree of curvature

$$\begin{array}{l} \text{Da}^\circ \\ 360^\circ \end{array} \begin{array}{l} \swarrow \\ \searrow \end{array} \begin{array}{l} 10 \text{ m} \\ 2\pi R \end{array}$$

$$\text{Da}^\circ = \frac{3600}{2\pi R}$$

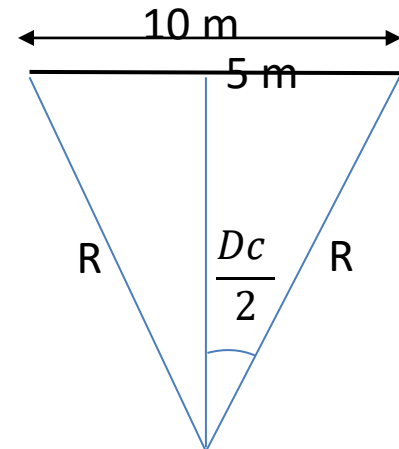
$$\text{Da}^\circ = \frac{573}{R}$$



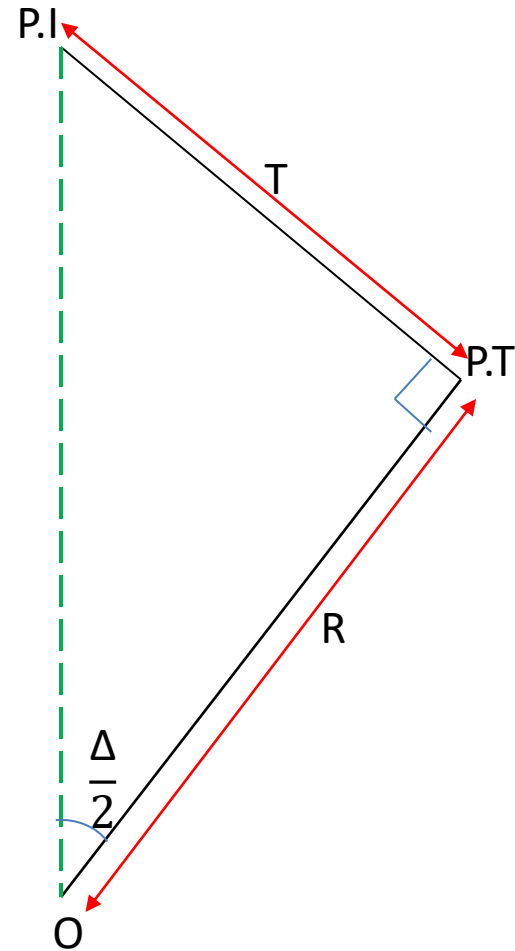
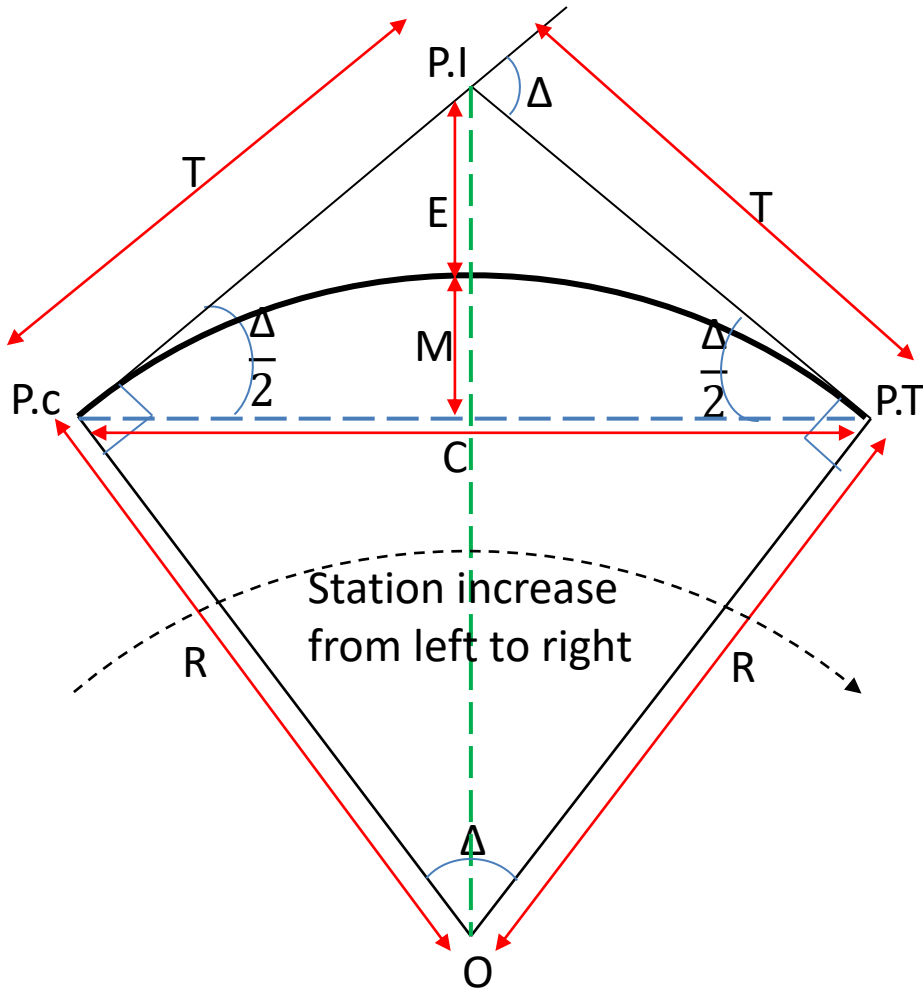
Degree of curvature

$$\sin D_c^{\circ} = \frac{5}{R}$$

$$D_c^{\circ} = \sin^{-1} \left(\frac{5}{R} \right)$$



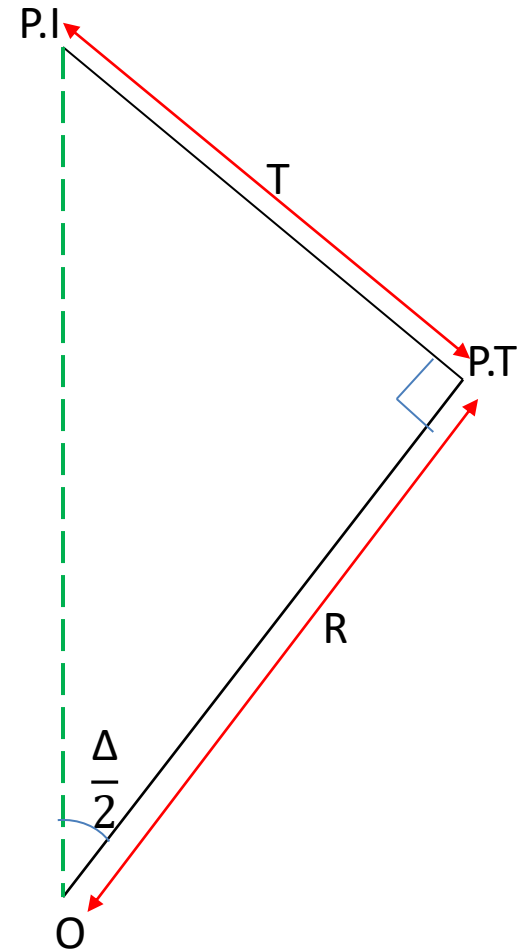
Tangent length



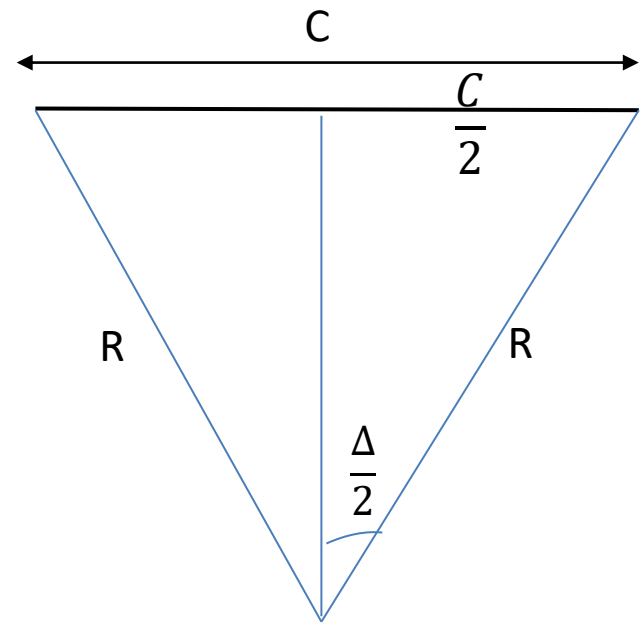
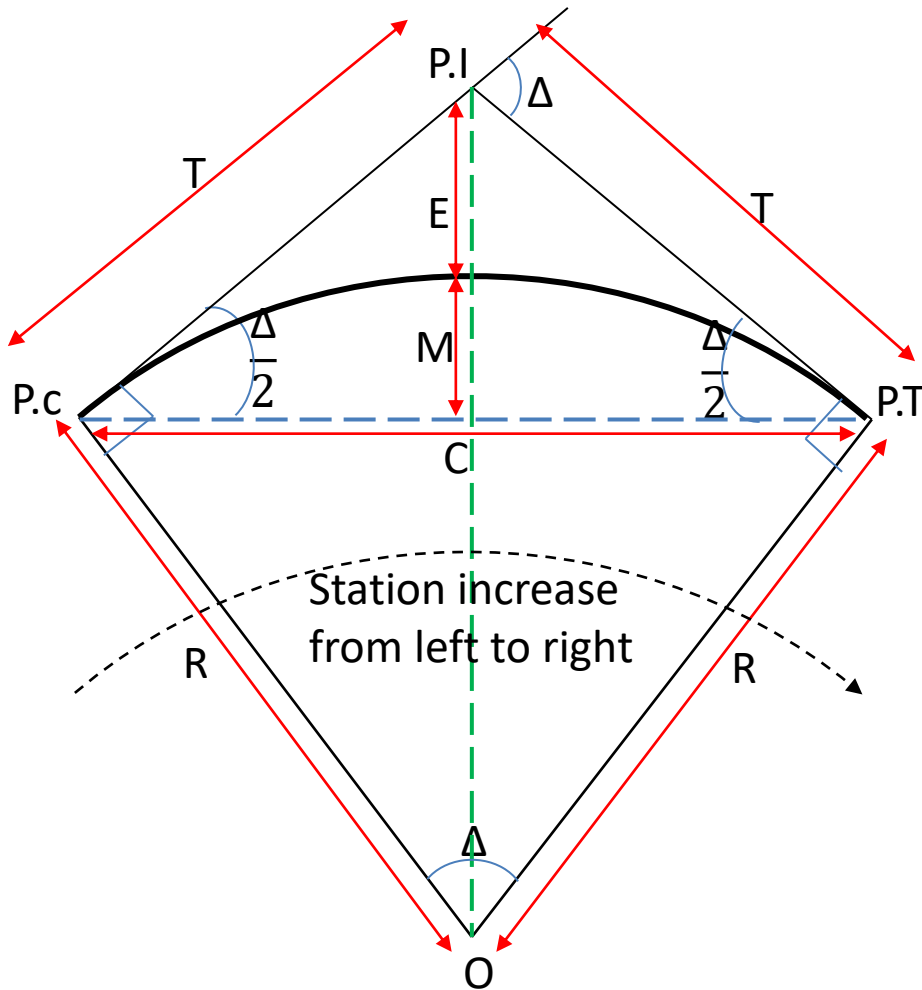
Tangent length

- $\tan \frac{\Delta}{2} = \frac{T}{R}$

$$T = R * \tan \frac{\Delta}{2}$$



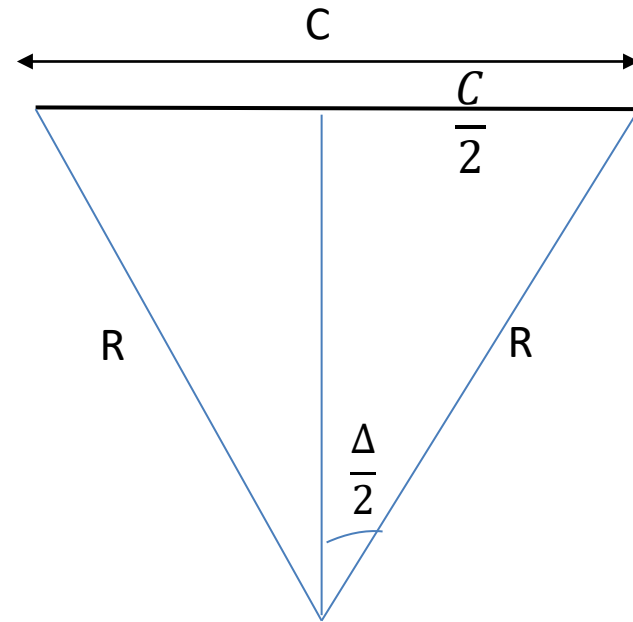
Chord length



Chord length

- $\sin \frac{\Delta}{2} = \frac{\frac{C}{2}}{R}$

$$C = 2 * R * \sin \frac{\Delta}{2}$$



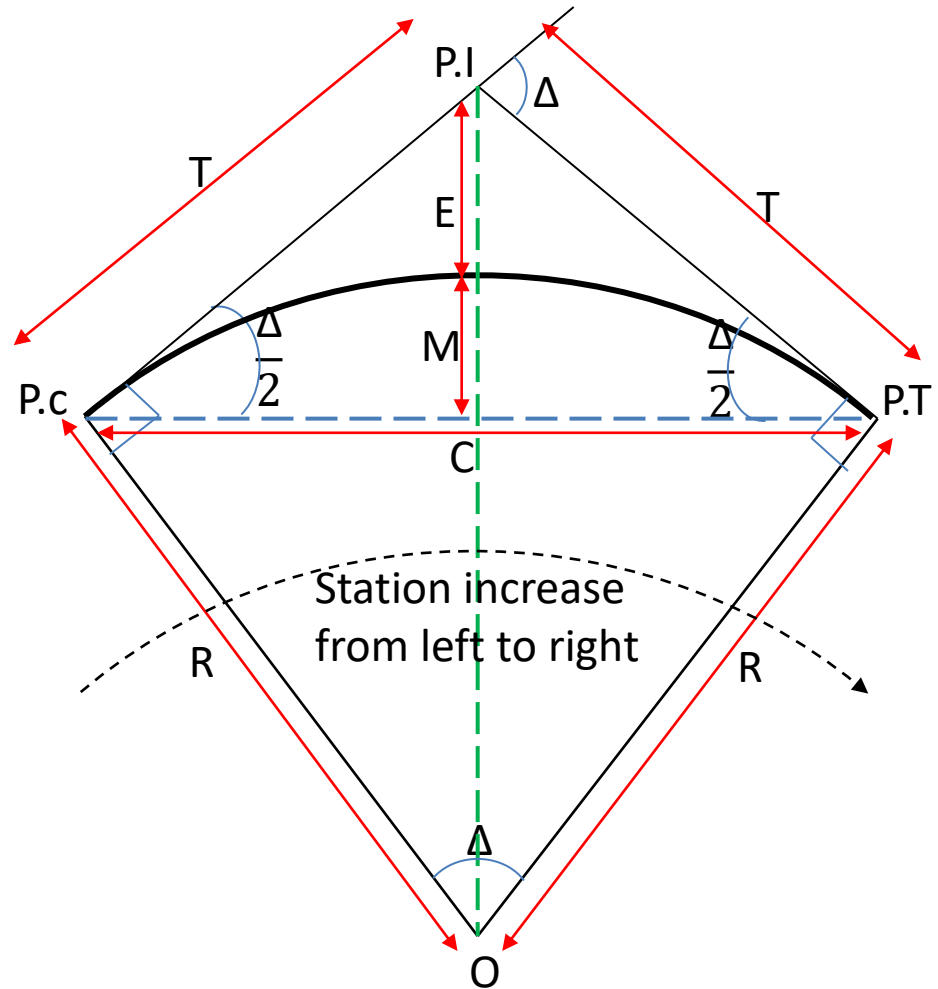
length of curve

- Δ \swarrow L
- 360° \swarrow $2\pi R$
- $L = \frac{\pi \cdot R \cdot \Delta^\circ}{180^\circ}$

$$L = R * \Delta_{\text{rad}}$$

$$\frac{L}{\Delta^\circ} = \frac{10}{D^\circ}$$

$$L = 10 * \frac{\Delta^\circ}{D^\circ}$$

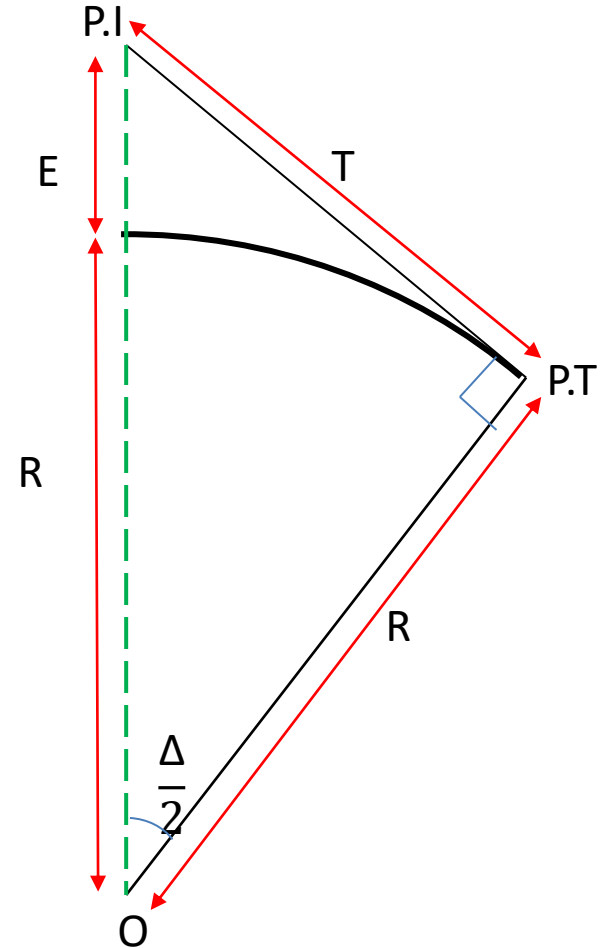


External distance

- $\cos \frac{\Delta}{2} = \frac{R}{R+E}$

$$E = R \left(\frac{1}{\cos \frac{\Delta}{2}} - 1 \right)$$

$$E = T \cdot \tan \frac{\Delta}{4}$$

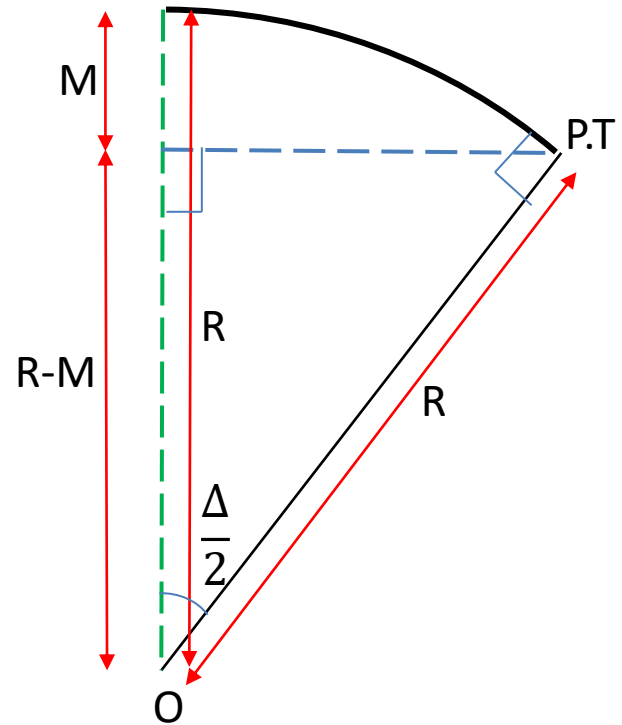


Middle distance

- $$\cos \frac{\Delta}{2} = \frac{R-M}{R}$$

$$M = R \left(1 - \cos \frac{\Delta}{2} \right)$$

$$M = R \left[1 - \sqrt{1 - \left(\frac{C}{2R} \right)^2} \right]$$



Stations

- Stat. P.C = Stat. P.I - T
- Stat. P.T = Stat. P.C + L
- $2T > L > C$

Example

- Compute the elements of the simple circular curve if you know:
- $R=250$ m , $\Delta=52^{\circ}36'$ and station of P.I.=14 + 80

- $Da^{\circ} = \frac{573}{R} = \frac{573}{250} = 2.292^{\circ} = 2^{\circ}17'31''$

$$Da^{\circ} = 2^{\circ}18'$$

- $T = R * \tan \frac{\Delta}{2} = 250 * \tan \frac{52^{\circ}36'}{2}$

$$T = 123.56 \text{ m}$$

- $C = 2 * R * \sin \frac{\Delta}{2} = 2 * 250 * \sin \frac{52^{\circ}36'}{2}$

$$C = 221.54 \text{ m}$$

- $L = \frac{\pi * R * \Delta^{\circ}}{180^{\circ}} = \frac{\pi * 250 * 52^{\circ}36'}{180^{\circ}}$

$$L = 229.51 \text{ m}$$

- $E = R \left(\frac{1}{\cos \frac{\Delta}{2}} - 1 \right) = 250 \left(\frac{1}{\cos \frac{52^{\circ}36'}{2}} - 1 \right)$

$$E = 28.87 \text{ m}$$

- $M = R \left(1 - \cos \frac{\Delta}{2} \right) = 250 \left(1 - \cos \frac{52^{\circ}36'}{2} \right)$

$$M = 25.88 \text{ m}$$

- $\text{Stat. P.C} = \text{Stat. P.I} - T = (14+80) - (1+23.56)$

$$\text{Stat. P.C} = (13+56.44)$$

- $\text{Stat. P.T} = \text{Stat. P.C} + L = (13+56.44) + (2+29.51)$

$$\text{Stat. P.T} = (15+85.95)$$

- $2T > L > C$